Annual WWW Technical Progress Report on the GDPS 2001

Country: Germany Centre: NMC Offenbach

1. Summary of highlights

The modelling suite at DWD consists of the global icosahedral-hexagonal gridpoint model GME (average mesh size ~ 60 km, i.e. 163842 gridpoints/layer, 31 layers) and the nonhydrostatic limited-area "Lokal-Modell" LM (mesh size ~ 7 km, 325 x 325 gridpoints/layer, 35 layers). LM is used operationally at the national meteorological services of Greece, Poland and Switzerland and at the regional meteorological service in Bologna (Italy), too.

The hydrostatic high-resolution regional model HRM of the DWD is being used as operational model at nine national/regional meteorological services, namely Brazil-INMET, Brazil-Navy, China, Israel, Italy, Oman, Romania, Spain and Vietnam. For lateral boundary conditions, GME data are sent via the Internet to the HRM and LM users.

During the year 2001 the main improvements of the NWP suite included:

- 20/03/01: Production of the GME run up to 174h based on a data cut-off of 2h 14min instead of 3h 40min. The previous "early run" of GME up to 78h with a data cut-off of 2h 14min has been stopped.
- 05/04/01: A prognostic turbulent kinetic energy (TKE) equation and an improved derivation of near surface variables have been introduced in LM.
- 18/06/01: Aircraft data (AMDAR) are being used in the nudging data assimilation scheme of LM.
- 29/08/01: A sea state model for the Mediterranean Sea (MSM) with a mesh size of 0.25° x 0.25° driven by 10m winds of GME has been added to the operational suite. MSM provides sea state forecasts up to 174h based on 00 and 12 UTC analyses.

A new high performance computer at DWD has been installed in the autumn of 2001. The IBM RS/6000 SP consists of 80 nodes with 16 processors each. The processors are equipped with a 375 MHz CPU (Power 3-II). Most of the nodes possess 8 GByte of shared memory, some possess 16 Gbyte. The peak performance of the total 80 node system (1280 processors) is around 2 Teraflop/s. The operational NWP suite will be fully ported to this new computer platform until the first quarter of 2002.

2. Equipment in use

2.1 Main computers

2.1.1 CRAY J932 (Operating system UNICOS)

32 CPUs with 8 GBytes memory, cycle speed 10 ns Peak performance in one CPU 200 Mflops 4 seperate IO-Clusters 160 GBytes of diskspace Access to STK ACS

Used for research

2.1.2 CRAY T3E (Operating system UNICOS/mk)

Processor cycle speed is 1.667 ns
776 Processors with 128 Mbytes memory
8 Processors with 1024 Mbytes memory
32 Processors with 512 MBytes memory
1024 GBytes of diskspace

Used for research and for operational forecasts

2.1.3 ORIGIN 2000 (Operating System IRIX)

System of four ORIGIN 2000 servers
70 Processors, cycle speed 4 ns
62 GBytes memory
8627 GBytes of diskspace
Access to STK ACS (3490E, SD3-Drives, 9840-Drives)

The system consists of servers for development, pre- and postprocessing, file distribution, Hierarchical Storage Management and the Oracle Database Implementation at DWD.

2.2 Networks

2.2.1 Ethernet

Connects Workstations, X-Terminals and PC's via router to the CRAYs and the ORIGIN 2000 servers

2.2.2 FDDI

Connects the Telecommunication System and the CRAYs.

2.2.3 **HIPPI**

The CRAYs and the ORIGIN 2000 servers are connected by HIPPI via a HIPPI-switch.

2.2.4 ATM

Access from the LAN to the ORIGIN 2000 systems is done via routers to the ATM-connected computers.

2.3 Special systems

2.3.1 Satellite data system

Microvax 4000-300 (Operating system VMS)

Used for preparation of satellite pictures (from METEOSAT and NOAA), vertical profiles of temperature and humidity (from NOAA).

2.3.2 Interactive graphical system

A number of SGI work stations and colour plotters are used for presentation of satellite- and radar data as well as model output, surface forecast charts significant weather charts, and other interactive graphics,

The MAP (Meteorological Application and Presentation System) Workstation is used to display and animate all available meteorological data sources.

2.3.3 Telecommunication system

Stratus continuum and X.25-switches Used for connections to GTS, ECMWF, EUMETSAT, national PTT network.

3. Data and products from GTS in use

At present nearly all observational data from the GTS are used. GRIB data from the France and GRIB data from the UK, the US and the ECMWF are used. In addition most of the MOTNE data are used as well. In addition most of the OPMET data are used.

Typical figures for 24 hours are:

SYNOP, SHIP	53.000 reports,
TEMP, part A	1.100 reports,
METAR	32.000 reports,
PILOT, part A	600 reports,
AIREP, AMDAR	28.000 reports,
SATEM, part A	11.000 reports,
SATOB, section 2	240.000 reports,
SATOB, section 3	6.000 reports,
SATOB, section 4	4.300 reports,
SATOB, section 5	68.000 reports,
SATOB, section 7	20.000 reports,
GRIB	7.500 bulletins,
BUFR	700 bulletins

4. Data input system

Fully automated system. Incoming reports in character orientied code forms are converted into BUFR before storing them into a data base.

5. Quality control system

There is no quality control system in use regarding outgoing data to the GTS except for formal structure.

5.1 Quality control of incoming data

The formats of all coded reports are checked and if necessary and possible corrected. Surface and upper air reports are checked for internal consistency before storing them into a data base.

6. Monitoring of the observing system

Surface observations and upper air observations are monitored quantitatively only on the national level. DWD acts as a lead centre for monitoring the surface observations in Region VI. At present, only the surface pressure observational data are checked.

7. Forecasting systems

7.1 System run schedule and forecast ranges

Preprocessing of GTS-data runs on a quasi-real-time basis about every 6 minutes on the ORIGIN 2000.

Independent 4-dim. data assimilation suites are performed for both models, GME and LM. For the GME, analyses are derived for the analysis times 00, 06, 12 and 18 UTC based on an intermittent optimum interpolation scheme. For the LM, a continuous data assimilation system based on the nudging approach provides analyses at hourly intervals.

The early forecast runs of GME and LM with a data cut-off of 2h 14 min after the main synoptic hours 00, 12 and 18 UTC consist of 48-h forecasts for LM and 78-h forecasts of the GME. They provide early numerical guidance to the Central Forecasting Office. In parallel to the early runs, a local sea state model (LSM, 3rd generation WAM) provides forecasts for North, Baltic and Adriatic Sea areas. The main forecast runs have a data cut-off of 3 h 30 min after the main synoptic hours 00 and 12 UTC and consist of 174-h forecasts of the GME and a global sea state model (GSM, 3rd generation WAM).

7.2 Medium range forecasting system (4-10 days)

7.2.1 Data assimilation, objective analysis and initialization

As far as GME is in use for medium range forecasting, the same procedures are applied as for short range forecasting described in item 7.3.1.

7.2.2 Model

Medium range forecasts at the DWD are mainly based on the ECMWF system (deterministic model and EPS). Additionally, GME (see 7.3) forecasts up to 7 days augment the model guidance available.

7.2.3 Numerical weather prediction products

ECMWF and GME global forecasts are available up to day 7. The ECOMET catalogue of the DWD global model products is given in annex 1.

7.2.4 Operational techniques for application of NWP products

A statistical interpretation scheme is applied to ECMWF and GME forecasts to provide medium-range forecasts for some German areas up to day 7. The scheme is based on the PPM philosophy. The interpretation results based on ECMWF and GME forecasts are averaged because verification results show that this average scores significantly better than each single model interpretation. Such a simple averaging proves to be a cost effective approach to reduce both the error and the error variance in medium-range forecasts (simplest ensemble prediction). The forecast parameter derived are:

Daily maximum and minimum temperatures, relative sunshine duration, daily precipitation amount and probability, wind speed and direction, probability of thunderstorm, probability of fog.

A new method to produce medium range forecasts in plain language for the public which had been introduced in 1999 was further developed and adapted to user requirements in the years 2000 and 2001. It allows for a centralized medium-range forecast activity. For this purpose a particular software was developed by DWD, which produces texts automatically from a data base. The data base is derived from the scheme described above. Every day in the beginning of the forecast business the meteorologist examines and — where necessary — postprocesses the data base and only then the text gen-

erator will be started. The automatically produced texts contain all significant weather parameters like cloud cover, precipitation, wind and extreme temperatures. In addition to this the automatic text production is in use for worldwide forecasts, which are available by dialling a premium rate number on a fax machine, on a telephone answering device or on mobile telephones using short message system (SMS). The latter ones are produced however without forecasters' intervention.

First steps were made in medium range forecasting concerning a risk assessment of extreme weather for the forecast interval 120 hours down to 24 hours by a very simple and subjective interpretation of EPS results.

Agrometeorological forecasts cover a wide span of applications aiming at a reduction of the use of insecticides and fungicides or at an optimization of the water supply to plants. NWP results are combined with additional models which calculate the drying of leaves or the temperature and water balance in the ground.

7.3 Short-range forecasting system (0-72 hrs)

Operational short-range forecasting is based on the products available from GME and LM, where LM covers the time period up to 48 h only.

The short-range forecasts for Central Europe up to 48 hours are derived from the limited-area "Lokal-Modell" LM. Fig. 1 shows the model domain of LM and Fig. 2 the model levels. The LM is designed as a flexible tool for forecasts on the meso-β and on the meso-γ scale as well as for various scientific applications down to grid spacings of about 100 m. For operational numerical weather prediction, LM is nested in the GME.

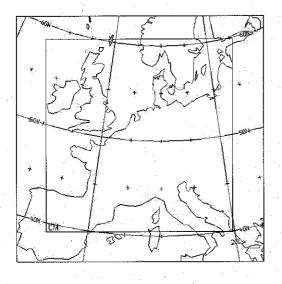


Figure 1 Model domain of the "Lokal-Modell" LM mesh size ~ 7 km, 325 x 325 gridpoints.

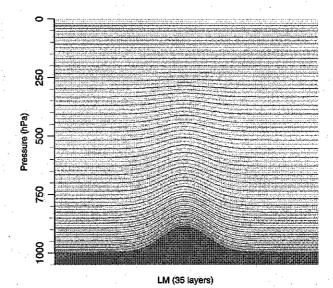


Figure 2 Model layers of LM.

7.3.1 Data assimilation, objective analysis and initialization

Global Model (GME)

a) Global analysis of mass, wind field and humidity

The program for the global analysis of mass and wind field, formerly developed by ECMWF, was ported to MPP systems by DWD with the support of the PALLAS software house.

Analysis method 3-dimensional multivariate optimal interpolation (humidity 2-dimensional).

Direct use of thickness data. Box method.

Analysed variables Φ, u, v, Rel. Hum.

Horizontal anal. grid icosahedral grid of the GME (average mesh size of 60 km)

Vertical resolution 31 hybrid layers (see GME)

Products a) On icosahedral-hexagonal grid of the GME

(163842 gridpoints/layer, 31 layers)

Variables: p_s, T, u, v, q_v, q_c

b) On a regular geographical grid, 480 x 361 points (0.75° x 0.5°)

12 pressure levels 1000, 950, 850, 700, 500, ..., 50 hPa

Variables: p_{msl} , T, Φ , u, v, Rel. Hum.

Assimilation scheme Intermittent data assimilation. Insertion of data every 6 hours.

6-h forecast used as first guess. All observations within a \pm 1.5-h window

used as synoptic.

Cut-off time 2 h 14 min.

Incremental digital filtering initialization (Lynch, 1997) consisting of

a 3-h adiabatic backward run and a 3-h diabatic forward run centered

at the initial time. The filtering is performed in vertical mode space; only the

external mode plus the first nine internal ones are filtered.

b) Global analysis of surface parameters

Analysis method Correction method

Analysed variables Sea surface temperature (SST) and snow cover

Horizontal anal. grid On icosahedral-hexagonal grid of the GME (average mesh size of 60 km)

Data used SST: Synop-Ship, US-SST analysis as background, US-data of ice border.

Snow cover: Snow depth, present and past weather, precipitation amount, temperature analysis. History taken into account. US-data of ice border.

Local Model (LM)

a) Limited-area analysis of atmospheric fields

The data assimilation system for the LM is based on the observation nudging technique (*Schraff*, 1997). The variables nudged are the horizontal wind, temperature, and humidity at all model layers, and pressure at the lowest model level. The lateral spreading of the observational information is horizontal, or optionally along model layers or isentropic surfaces. At present, the scheme uses only conventional data of type TEMP, PILOT, SYNOP, BUOY, AIRCRAFT and AMDAR.

Analysis method Observation nudging technique

Analysed variables p, T, u, v, Rel. Hum.

Horizontal anal. grid 325 x 325 points (0.0625° x 0.0625°) on a rotated latitude/longitude grid

Vertical resolution 35 hybrid layers (see LM)

Products All analysis products are given on the 325 x 325 grid and available at

hourly intervals.

a) On the 35 LM layers Variables: p, T, u, v, w, q_v, q_c

b) On 10 pressure levels (1000, 950, 850, 700, 500, ..., 200 hPa) Variables: p_{msl} , Φ , T, u, v, ω , Rel. Hum.

c) On 4 constant height levels (1000, 2000, 3000, 5000 m) Variables: p, T, u, v, w, Rel. Hum.

Assimilation scheme Continuous data assimilation. Insertion of data in 3-h cycles.

Cut-off time 2 h 14 min for LM runs.

Initialization None

b) Limited-area analysis of soil moisture

Analysis method 2-dimensional (vertical and temporal) variational technique

Analysed variables soil moisture of 2 soil layers at 00 UTC

Horizontal anal. grid 325 x 325 points (0.0625° x 0.0625°) on a rotated latitude/longitude grid

Data used 2-m temperature analyses at 12 and 15 UTC

c) Limited-area analysis of other surface parameters

Analysis method Correction methods

Analysed variables Sea surface temperature (SST) and sea ice cover, snow cover

Horizontal anal. grid 325 x 325 points (0.0625° x 0.0625°) on a rotated latitude/longitude grid

Data used SST: Synop-Ship, US-data of ice border, sea ice cover analysis from BSH

(German Institute for shipping and hydrology) for the Baltic Sea and indirectly

satellite data (via NCEP-SST and GME SST analyses).

Snow cover: Snow depth, present and past weather, precipitation amount,

2-m temperature analysis (plus model prediction).

Additionally, the plant cover is derived on a weekly basis by evaluation of satellite data (NDVI index).

7.3.2 **Model**

7.3.2.1 Schematic summary of the global model GME

Domain Global

Initial data time 00, 12, 18 UTC

Forecast range 174 h (from 00 and 12 UTC), 48 h (from 18 UTC)

Prognostic variables p_s , T, u, v, q_v , q_c

Vertical coordinate hybrid sigma/pressure (Simmons and Burridge, 1981), 31 layers

Vertical discretization Finite-difference, energy and angular-momentum conserving

Horizontal grid Icosahedral-hexagonal (Sadourny et al., 1968), mesh size between

55 and 65 km, average mesh size 60 km; Arakawa-A grid

Horiz. discretization Finite-difference, second order

Time integration 3-time-level, leapfrog, split semi-implicit scheme, $\Delta t = 4$ min, time filter.

For moisture variables (water vapour, cloud water): Positive-definite, shape-

preserving horizontal advection (SL-scheme).

Horizontal diffusion Linear, fourth order

Orography Grid-scale average based on a 1-km data set

Parameterizations Surface fluxes based on local roughness length and stability (*Louis, 1979*)

Free-atmosphere turbulent fluxes based on a level-two scheme

(Mellor and Yamada, 1974)

Sub-grid scale orographic effects (blocking and gravity wave drag) based

on Lott and Miller, 1997

Radiation scheme (two-stream with two solar and five longwave intervals) after *Ritter and Geleyn (1992)*, full cloud-radiation feedback based on predicted clouds

Mass flux convection scheme after Tiedtke (1989)

Kessler-type grid-scale precipitation scheme with parameterized cloud microphysics

Two-layer soil model (*Jacobsen and Heise, 1982*) including simple vegetation and snow cover; prescribed climatological values at about 40 cm depth for temperature and at 100 cm depth for soil moisture.

Over water: Fixed SST from SST analysis; roughness length according to Charnock's formula

Analyses and forecasts (up to 78 h) data of GME are sent twice daily (for 00 and 12 UTC) via the Internet to several other national weather services (e. g. Brazil, , China, Greece, Israel, Italy, Oman, Poland, Romania, Spain, Switzerland, Vietnam). These data serve as initial and lateral boundary data for regional modelling. For a detailed description of GME, see *Majewski*, 1998 and *Majewski* et al., 2002.

7.2.3.2 Schematic summary of the "Lokal-Modell" LM

Domain Central Europe

Initial data time 00, 12, 18 UTC

Forecast range 48 h

Prognostic variables p, T, u, v, w, q_v, q_c TKE

Vertical coordinate Generalized terrain-following, 35 layers (see Fig. 2)

Vertical discretization Finite-difference, second order

Horizontal grid 325 x 325 points (0.0625° x 0.0625°) on a rotated latitude/longitude grid,

mesh size 7 km; Arakawa-C grid, see Fig. 1.

Horiz discretization Finite-difference, second order

Time integration Three-time-level, leapfrog, split explicit scheme (Klemp and

Wilhelmson, 1978) with the extensions proposed by Skamarock and Klemp (1992), $\Delta t = 40$ s, time filter.

Optionally, a two-time-level split-explicit scheme (*Wicker and Skamarock, 1998*) and a 3-d semi-implicit scheme (*Skamarock et al., 1997*) are available.

Horizontal diffusion Linear, fourth order

Orography Grid-scale average based on a 1-km data set. Topography has been filtered to

remove grid-scale structures

Parameterizations Surface fluxes based on local roughness length and stability (Louis, 1979)

Free-atmosphere turbulent fluxes based on a level-2.5 scheme with prognostic

TKE (Mellor and Yamada, 1974)

Radiation scheme (two-stream with two solar and five longwave intervals) after *Ritter and Geleyn (1992)*, full cloud-radiation feedback based on

predicted clouds

Mass flux convection scheme after Tiedtke (1989)

Kessler-type grid-scale precipitation scheme with parameterized cloud

microphysics

Two-layer soil model (Jacobsen and Heise, 1982) including simple vegetation and snow cover; prescribed climatological values at about 40 cm depth for temperature and at 100 cm depth for soil moisture.

Over water: Fixed SST from SST analysis; roughness length according to Charnock's formula

7.3.3 Numerical weather prediction products

Short-range forecasts are based on direct model output (DMO) of the LM and on statistically corrected values (simple Kalman filtering). MOS guidance based on GME data is provided, too. The ECOMET catalogue of the LM is given in annex 2.

7.3.4 Operational techniques for application of NWP products

NWP results are used for a variety of further applications. Some of these applications are briefly described below.

Short range forecasts of weather and temperature in pictorial form are automatically produced for online presentation on the Internet using Kalman filtered forecasts of both GME (worldwide) and LM (national).

The state of road surfaces is predicted by a road weather forecast system (SWIS – Strassenzustandund Wetter-Informations-System) using Kalman filtered forecasts of the "Lokal-Modell" LM and an energy balance model of the road surface.

The influence of weather on human health is forecasted using a bio-synoptical weather classification scheme and the predicted vorticity, temperature and humidity. The thermal stress on a prototype human being is calculated with an energy balance model which additionally employs forecasted wind and cloudiness.

Agrometeorological forecasts cover a wide span of applications aiming at a reduction of the use of insecticides and fungicides or at an optimization of the water supply to plants. NWP results are combined with additional models which calculate the drying of leaves or the temperature and water balance in the ground.

Significant weather charts which are in use as general guidance for the aeronautical consulting business in the regional forecasting offices and which are issued as products for general aviation cover the middle european area in a layer from surface up to 24 500 ft. As additional information jet-axes and

cat areas are included if within the layer. Icing conditions and turbulence areas are described. The charts are produced interactively on work stations using LM results in combination with conventional synoptic methods.

During the season an advice for gliding pilots is prepared which may be received via facsimile. It presents charts of the lowest cloud base or the height of thermal activity, precipitation, wind direction and wind speed for several times during the day. It is based on LM data.

During the summer months an UV-B index is evaluated using predicted stratospheric temperatures, TOVS data, and a high resolution radiation model.

7.4 Specialized forecasts

7.4.2 Models

7.4.2.1 Trajectory Models

Trajectory model:

Forecast variables $r(\lambda, \phi, p \text{ or } z, t)$

Data supply u, v, w, p_s from NWP forecasts (or analyses)

Numerical scheme 1st order Euler-Cauchy with iteration (2nd order accuracy) Interpolation 1st order in time, 2nd (GME) or 3rd (LM) order in space

a) Daily routine (ca. 1500 trajectories)

Trajectories based on LM forecasts:

Domain of LM (see Fig. 1)

Resolution 0.0625° (as LM)
Initial data time 00, 12 UTC

Trajectory type Forward trajectories for 36 German, Czech, Swiss, and French

nuclear and chemical installations, backward trajectories for scientific

investigations

Forecast range 48-h trajectories, optional start/arrival levels

Trajectories based on GME forecasts:

Domain Global

Resolution ~ 60 km (as GME) Initial data time 00, 12 UTC

Trajectory type 72-h forward trajectories for ca. 60 European nuclear sites and 8 Ger-

man regional forecast centers, backward trajectories for 37 German radioactivity measuring sites and 8 forecast centers using consecutive

+6h to +18h forecast segments.

96-h backward trajectories for the GAW mountain stations Zugspitze, Jungfraujoch, Sonnblick and Hohenpeißenberg, and to the German meteorological observatories.

72-h backward trajectories for 5 African cities in the framework of the METEOSAT-MDD program, disseminated daily via satellite from Bracknell.

120-h backward trajectories for the German polar stations Neumayer (Spitzbergen) and Koldewey (Antarctica) and the research ships Polarstern and Meteor, disseminated daily.

168-h forward trajectories for 14 Eastern European nuclear power

plants.

Mainly backward trajectories for various scientific investigations. 168h forward and backward trajectories, optional start/arrival levels

Forecast range

b)

Operational emergency trajectory system, trajectory system for scientific investigations:

Models LM or GME trajectory models

Domain LM or global

Data supply u, v, w, p_s from LM or GME forecasts or analyses, from current data

base or archives

Trajectory type Forward and backward trajectories for a choice of offered or freely

eligible stations at optional heights and times in the current period

of 7 to 14 days.

Forecast range 48-h (LM) or 168-h (GME)

Mode Interactive menu to be executed by forecasters

7.4.2.2 Sea wave models

Domain	Global	North, Baltic and Adriatic Sea Areas					
Numerical scheme	Deep water, 3 rd generation WAM	Deep water, 3 rd generation WAM					
Wind data supply	GME: u, v at 10 m	LM and GME: u, v at 10 m					
Grid	geographical (regular lat/lon)	geographical (regular lat/lon)					
Resolution	0.75° x 0.75°	0.167° x 0.10°					
Initial data time	00 and 12 UTC	00 and 12 UTC					
Forecast range	174 h	48 h					
Model output	significant wave heig	ht, frequency, direction					
Initial state	sea state adapted to analysed wind field over last 12						
Verification	ion Available on request						

7.4.3. Numerical Weather Prediction Products

The forward and backward trajectories are an important tool for emergency response activities. In addition to these forecasts for concentration and deposition of radionuclides are produced using a Lagrangian Particle Dispersion Model.

Based on the Sea wave models charts are produced for swell and significant wave height, frequency and direction .

7.4.4 Operational techniques for applications of NWP results

Forecasts of the optimal (shortest and/or safest) route of ships are evaluated using the results of the global sea wave model and of NWP in the ship routing modelling system of the DWD. The system calculates isochrones taking into account the impact of wave and wind on different types of ships.

A very special application of the NWP result is a hydrological one. A model-system called SNOW-D allows for estimating and forecasting snow-cover development and areal melt water release. The model enables a daily calculation and forecast of grid-point values of the water equivalent of the snow cover and meltingwater release. The snow cover development is computed with the help of physically-based model components which describe accumulation (build-up, increase), metamorphosis (conversion, change) and ablation (decrease, melting).

The model input data are

- 6-hour interval averages of air temperature and vapour pressure
- global radiation/duration of sunshine and precipitation totals of the last 24 h
- three times a week additional data from a part-time network (depth of snow cover, water equivalent of snow cover)
- output data of the "Lokal-Modell"

The model output contains

- current values of the snow cover (reference point 06.00 UTC)
 - snow depth (in cm)
 - water equivalent (in mm)
- specific water equivalent (in mm/cm)
- forecast values of snow cover development (forecast interval maximum 48 hours, forecasting for 6-h-intervals)
 - water equivalent (in mm)
 - precipitation supply, defined as the sum of meltwater release and rain (in mm)

The results are provided grid-oriented and with a blanket coverage for Germany. A summary of the grid values can be made for any area required.

In addition to SNOW-D, a new model-system called SNOW-BW was developed for Baden-Württemberg and will be extended to Rhineland-Palatinate in 2002. This model is similar to SNOW-D but it runs every 6 hours and has a higher temporal resolution (1 hour). Not only DWD measurements but also data from regional networks (UMEG) are integrated in the data sampling procedure. Universal Kriging is used for regionalization of measured values to the computational grid.

The strongly improved physics uses wind speed (which is neglected in SNOW-D) for computation of turbulent transfer of heat and moisture taking into account the atmospheric static stability. The model output contains the quantities of SNOW-D but in addition forecast values of snow depth, snow temperature, ice content and so on can be derived.

8. Verifications

Tables 1 up to 6 show verification results of GME for the european region $(36^{\circ} - 72^{\circ} \text{ N}, 12^{\circ}\text{W} - 42^{\circ}\text{E})$, tables 7 up to 12 for the extratropical northern hemisphere and tables 13 up to 18 for the extratropical southern hemisphere. In all tables forecast times vary from 12 h up to 156 h in intervals of 24 hours. P156.h stands for the RSME-values of persistence and climate for the rsme-values of climate.

8.1 European Region

Table 1		GEOP	OTE	NTIA	L 5	00 hF	'a	RMS	SE				
12.h	Jan . 9	Feb 10	Mar 9	Apr 8	May 8	Jun 7	Jul 8	.Aug 7	Sep.	Oct 8	Nov 10	Dec 10	Mean 8.5
36.h	19	21	19	19	17	15	16	14	17	19	23	20	18.1
60 h	30	35	29	31	26	25	. 26	22	29	30	41	34	29.9
84.h	.45	50	43	47	39	36	35	33	41	42	57	52	43.4
108.h	65	71	56	64	56	50	44	45	. 52	61	76	71	59.3
132.h	86	89	70	81	73	62	54	55	72	81	100	93	76.4
156.h	106	105	81	100	86	72	61	62	90	90	119	109	90.2
p156.h	172	219	125	141	135	102	102	97	120	137	160	203	142.7
climate	137	161	90	108	121	86	84	74	112	117	136	184	117.5

Table 2	G	EOP	OTEN	TIAI	500	hPa	7 7	AN	OMA	LYC	ORR	ELAT	ION
	Jan .	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov.	Dec	Mean
12.h	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	0.997
36.h.	0.99	0.99	0.98	0 98	0.99	0.98	0.98	0.98	0.98	0.98	0.98	0.99	0.983
60.h	0.97	0.96	0.94	0,.95	0.97	0.94	0.94	0.94	0.96	0.95	0.95	0.97	0.954
84.h	0.94	0.92	0.88	0.88	0.94	0.88	0.89	0.86	0.92	0.90	0.90	0.93	0.902
108.h	0.85	0.85	0.80	0.79	0.88	0.76	0.8.0	0.74	0.86	0.79	0.82	0.87	0.818
132.h	0.75	0.76	0.70	0.68	0.80	0.63	0.70	0.62	0.74	0.62	0.69	0.79	0.707
156.h	0.66	0.65	0.60	0,53	0.72	0.50	0.66	0.55	0.59	0.55	0.60	0.73	0.611

Table 3		PRE	PRESSURE			MSL 1			RMSE				•
					•								
	Jan	Feb	Mar	Apr	Мау	Jun	Jul	Aug	Sep	Oct	Nov	Dec	Mean
12.h	1.1	1.2	1.0	0 9	0.9	0.8	0.8	0.9	0.9	1.0	1.2	1 1	0.98
36.h	2.2	2.3	2.1	2.0	1.7	1.5	1.7	1.5	1.5	1.9	2.4	2.1	1.91
60.h	3.2	3.6	3.1	3.1	2.5	2.4.	2.6	2.4	2.6	2.8	4.1	3.4	2.29
84.h	4.6	4.9	4.6	4.2	3.4	3.2	3.4	3.4	3.6	4.1	5.7	5.2	4.18
108.h	6.3	6.7	5.9	5.4	4.7	4.2	4.0	4.2	4.6	5 . 8	7.4	6.9	5.52
132.h	8.4	8.5	6.9	6.5	6.1	5.1	4.7	4.9	6.1	7.4	9.3	8.8	6.89
156.h	10.0	9.7	7.7	7.9	7.2	5.6	5.3	5.4	7.4	8.4	10.5	9 9	7.91
p156.h	17.6	16.5	11.0	11.2	9.8	7.0	7.9	6.9	9.9	11.5	13.9.	16.1	11.61
climate	12.9	12.4	8.6	7.2	7.3	5.1	5.6	5.3	8.8	8.6	11.9	14.8	9.03

Table 4	PRESSURE			MSL			ANOMALY CORRELATION					ION	
	Tan	Pob	Mari	Anr	Mass	Tun	Tis I	Aug	San	Oct	Nov	Dec	Mean
12.h													
36.h	0.98	0.98	0.97	0.96	0.97	0:96	0.95	0.95	0.98	0.97	0.97	0.98	0.968
60.h	0.96	0.94	0.92	0.90	0.93	0.90	0.89	0.88	0.95	0.93	0.92	0.95	0.922
													0.848
108.h													
132.h	-												
156.h	0.61	0.57	0,56	0.33	0.49	0.40	0.56	0.53	0.59	0.42	0.57	0.59	0.518

Table 5	TEMPERATURE			URE		850 h	Pa	RMSE					
12.h 36.h 60.h 84.h 108.h 132.h 156.h pl56.h	1.4 1.8 2.3 2.9 3.5 4.1 6.3	0.9 1.4 2.0 2.5 3.2 3.8 4.4 7.1	0.8 1.4 1.9 2.6 3.2 3.7 4.1 6.4	0.8 1.4 1.8 2.3 3.0 3.6 4.2 5.6	0.8 1.3 1.7 2.2 2.8 3.4 4.0 5.8	0.8 1.3 1.6 2.0 2.5 3.0 3.5 5.0	0.9 1.3 1.7 2.2 2.6 3.0 3.4 4.7	0.8 1.3 1.6 1.9 2.3 2.7 3.1 4.7	0.8 1.3 1.7 2.1 2.5 2.8 3.3 4.6	0.9 1.5 1.9 2.4 3.0 3.6 4.0 5.2	3.5 4.1 4.5 5.7	0.9 1.5 2.0 2.6 3.3 4.1 4.8 6.6	0.86 1.37 1.84 2.35 2.89 3.46 3.95 5.64

Table 6		TEMPERATURE					850 hl	Pa	ANOMALY CORRELATION					
	Jan-	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov.	Dec	Mean	
12.h	0.97	0.98	0.98	0.98	0.98	0.97	0.97	0.96	0.97	0.97	0.97	0.97	0.973	
36.h	0.92	0.94	0.94	0.94	0.96	0.93	0.93	0.91	0.93	0.93	0.93	0.93	0.932	
60.h	0.87	0.87	0.90	0.88	0.93	0.89	0.89	0.86	0.88	0.87	0.86	0.89	0.883	
84.h	0.81	0.81	0.82	0.81	0.89	0.81	0.82	0.79	0.82	0.80	0.77	0.83	0.815	
108.h	0.72	0.71	0.72	0.71	0.81	0.72	0.74	0.70	0.75	0.69	0.67	0.75	0.725	
132.h	0.59	0.59	0.63	0.60	0.71	0.60	0.65	0.59	0.68	0.54	0.52	0.63	0.610	
156.h	0.47	0.50	0.57	0.49	0.63	0.48	0.56	0.49	0.55	0.45	0.43	0.51	0.511	

8.2 Extratropical northern hemisphere

m-11-7		GEOPOTENTIAL 500 hPa RMSE											
Table 7		GE	OPO	ILNI	IAL	2	ou nr	а		CIMIST	2		
	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec	Mean
12.h	11	11	10	10	9	8	8	8	. 9	9	10	11	9.5
36.h	. 22	22	20	20	18	17	16	17	17	19	21	22	19.3
60.h	34	35	32	31	28	27	25	27	27	31	33	34	30.3
84.h	47	49 4	45	44	39	37	35	37	- 39	43	46	49	42.5
108.h	61	65	58	5,8	51	49	44	47	52	56	60	63	55.3
132.h	74	79	71	72	62	60	52	56	66	69	74	77	67.8
156.h	86	91	84	85	74	70	59	64	77	80	88	89	78.9
p156.h	129	146	137	125	106	99	- 85	91	105	116	127	146	117.7
climate	101	118	102	94	89	78.	68	70	88	94	108	130	95.0

Table 8		GEOPOTENTIAL			:	รบบ ทา	ra	. 1	ANON	COF	KKLLA	ı	
	Jan	Feb Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec	Mean	-
12.h	0.99	1.00 1.00	1.00	0.99	0.99	0.99	0.99	0.99	0.99	1.00	1.00	0.994	
36.h	0.97	0.98 0.98	0.98	0.98	0.97	0.97	0.97	0.98	0.97	0.98	0.98	0.976	
60.h	0.94	0.95 0.95	0.94	0.94	0.93	0.93	0.92	0.94	0.94	0.95	0.96	0.941	
84:h	0.88	0.91 0.90	0.88	0.89	0.87	0.86	0.84	0.89	0.87	0.90	0.92	0.884	
108.h	0.80	0.84 0.83	0.80	0.81	0.77	0.78	0.74	0.80	0.79	0.83	0.87	0.804	
132.h	0.71	0.76 0.73	0.68	0.72	0.65	0.69	0.62	.0.69	0.68	0.75	0.80	0.707	
156.h	0.62	0.67 0.63	0.56	0.61	0.53	0.59	0.51	0.58	0.59	0.64	0.74	0.606	
	7												

Table 9		PRE	SSUF	Œ		M	SL		R	MSE			
÷	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec	Mean
12.h	1.5	1.4	1.2	1.2	1.2	1.1	1.1	1.2	1.2	1.2	1.3	1.4	1.25
36.h	2.6	2.6	2 2	2.2	2.0	1.9	1.9	2.0	2.0	2.3	2.4	2.7	2.23
60.h	3.8	3.7	3.3	3.2	2.8	2.7	2.7	2.7	3.0	3.3	3.6	3.8	3.21
84.h	5.0	4.9	4.5	4.3	3.6	3.4	3.4	3.6	3.9	4.4	4.8	5.2	4.26
108.h	6.4	6.4	5.7	5.5	4.6	4.3	4.1	4.4	5.0	5.6	6.1	6.5	5.38
132.h	7.6	7.7	6.8	6.7	5.6	5.2	4.8	5.0	6.0	6.8	7.5	7.7	6.45
156.h	8.6	8.8	7.8	7.6	6.4	5.9	5.4	5.5	7.0	7.6	8.8	8.7	7.35
p156.h	12.8	13.2	13.0	10.2	8.9	7.9	7.0	7.2	9.2	10.6	11.6	12.4	10.34
climate	9.4	10.3	9.6	7.3	6.6	5.7	5.2	5.6	7.1	7.9	9.4	11.1	7.93

Table 10 PRESSURE MSL ANOMALY CORRELATION

 Jan
 Feb
 Mar
 Apr
 May
 Jun
 Jul
 Aug
 Sep
 Oct
 Nov
 Dec
 Mean

 12.h
 0.99
 0.99
 0.99
 0.98
 0.98
 0.97
 0.98
 0.98
 0.98
 0.98
 0.99
 0.99
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 0.99
 0.99
 0.95
 0.95
 0.96
 0.95
 0.90
 0.90
 0.90
 0.92
 0.93
 0.905
 84.h
 0.84
 0.81
 0.81
 0.77
 0.83
 0.83
 0.86
 0.81
 0.77
 0.83
 0.83
 0.84
 0.81
 0.78
 0.77

TEMPERATURE 850 hPa Table 11 **RMSE** Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec Mean 1.0 1.0 1.0 1.0 0.9 1.0 1.0 1.1 0.98 12.h 1.0 1.0 0.9 1.0 1.6 1.7 1.8 1.63 36.h 1.8 1.7 1.6 1.7 1.6 1.6 1.5 1.6 1.5 2.3 2.2 60.h 2.3 2.2 2.1 2.1 1.9 2.0 1.9 2.1 2,2 2.3 2.13 2.5 2.3 2.4 84.h 2.8 2.8 2.8 2.8 2.5 2.4 2.6 2.9 2.7 2.8 3.0 3.2 3.4 3.12 108.h 3.4 3.5 3.4 3.3 3.0 2.7 132.h 3.9 4.1 3.9 3.9 3.4 3.3 3.0 3.1 3.2 3.5 3.7 4.0 156.h 4.4 4.6 4.5 4.3 3.8 3.6 3.3 3.4 3.6 3.9 4.2 p156.h 6.0 6.3 6.3 6.2 5.5 4.9 4.4 4.6 5.0 5.4 6.0 6.0 5.55 4.8 4.8 4.5 3.7 3.3 3.4 4.0 4.4 4.8

Table 12 TEMPERATURE 850 hPa ANOMALY CORRELATION

 Jan
 Feb
 Mar
 Apr
 May
 Jun
 Jul
 Aug
 Sep
 Oct
 Nov
 Dec
 Mean

 12.h
 0.98
 0.98
 0.98
 0.97
 0.96
 0.96
 0.96
 0.97
 0.97
 0.98
 0.98
 0.971

 36.h
 0.93
 0.94
 0.94
 0.93
 0.92
 0.90
 0.89
 0.88
 0.91
 0.92
 0.93
 0.94
 0.920

 60.h
 0.87
 0.89
 0.89
 0.88
 0.87
 0.83
 0.81
 0.86
 0.85
 0.89
 0.89
 0.865

 84.h
 0.80
 0.83
 0.81
 0.76
 0.76
 0.73
 0.79
 0.78
 0.82
 0.84
 0.798

 108.h
 0.73
 0.74
 0.73
 0.74
 0.68
 0.69
 0.64
 0.71
 0.75
 0.77
 0.719

 132.h
 0.64
 0.65
 0.64
 0.67
 0.59
 0.61
 0.56
 0.62
 0.61

8.3 Extratropical southern hemisphere

Table 13	3	GEOPOTENTIAL			,	500 hPa			RMS	E ,			
	Jan	Feb	Mar	Apr	May		Jul	_		Oct	Nov	Dec	Mean
12.h	12	.11	13 -		14	15	16	16	15	14	13	13	13.8
36.h	26.	25	28	31	32	34	33 -	34	32	30	29	29	30.2
60:h	40	38	43	46	49	53	49	53	49	45	44	44	46.0
84.h	54	50	58	. 63	67	71	65`	70	64	59	58	56	61.2
108.h	6.6	64	74	79	83	89	81	85	. 78	73	71	67	75.7
132.h	78	76	88	92	96	102	96	98	90	82	83	77	88 3
156.h	90	85 `	100	104	107	116	108	111.	102	90	94	86	99.4
p156.h	99	116	131	130	138	143	146	133	131	134	116	118	127.8
climate	77	84	94	97	111	105	119	108	105	100	89	98	98.7

GEOPOTENTIAL 500 hPa ANOMALY CORRELATION Table 14 Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec Mean 36.h. 0.93 0.96 0.95 0.95 0.96 0.95 0.96 0.95 0.95 0.96 0.95 0.95 0.95 60.h 0.85 0.90 0.89 0.87 0.90 0.87 0.91 0.88 0.88 0.90 0.87 0.89 0.884 84.h 0.73 0.82 0.79 0.77 0.81 0.76 0.84 0.78 0.79 0.82 0.78 0.81 0.793 108.h 0.60 0.71 0.66 0.65 0.71 0.64 0.76 0.68 0.69 0.73 0.67 0.72 0.685 132.h 0.45 0.59 0.53 0.53 0.61 0.53 0.66 0.57 0.59 0.65 0.55 0.64 0.575 156.h 0.31 0.49 0.40 0.42 0.52 0.41 0.57 0.47 0.49 0.58 0.43 0.56 0.471 MSL Table 15 PRESSURE RMSE Sep Oct Nov Dec Apr May Jun Jul Aug Mean Jan Feb Mar 1.8 1.9 2.0 1.8 1.8 1.7 12.h 1.8 1.7 1.74 1.5 1.4 1.6 1.8 2.7 36.h 3.0 3.2 3.6 3 27 3.8 3.6 4.0 3.6 3.3 3.2 3.2 3.41 4.0 60.h 4.3 4 6 5.1 5.3 5.6 5.3 5.6 5.2 4.7 4.4 4.4 4.86 6.9 7.3 6.8 7.1 6.6 5.9 5.5 5.4 6.19 84.h 5.5 5.0 5.8 6.4 6.2 7.1 7.7 8.2 8.8 8.4 8.7 7.8 7.1 6.6 6.3 7.45 108.h 6.5 132.h 7.5 7.3 8.3 8.7 9.4 10.0 9.8 10.1 9.0 7.8 7.6 8.1 9.3 9.6 10.5 11.3 10.8 11.0 10.1 8.5 8.5 7.7 9.49 156.h 8.4 p156.h 9.0 9.5 11.6 11.5 13.0 13.2 13.9 12.4 12.1 11.6 10.1 10.2 11.51 7.2 8.6 8.7 10.7 10.2 11.2 10.2 9.7 8.9 8.1 8.4 9.05 climate 6.9 Table 16 PRESSURE MSL ANOMALY CORRELATION Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec Mean 36.h 0.89 0.93 0.93 0.91 0.93 0.92 0.94 0.92 0.92 0.93 0.91 0.92 0.922 60.h 0.79 0.84 0.84 0.81 0.86 0.84 0.88 0.84 0.84 0.86 0.83 0.86 0.841 $84.h \quad 0.67 \ 0.75 \ 0.74 \ 0.69 \ 0.77 \ 0.73 \ 0.80 \ 0.74 \ 0.75 \ 0.77 \ 0.74 \ 0.77 \ 0.744$ 108.h 0.54 0.63 0.61 0.58 0.67 0.61 0.69 0.62 0.65 0.67 0.63 0.69 0.634 132.h 0.40 0.51 0.50 0.47 0.58 0.50 0.59 0.50 0.55 0.59 0.52 0.61 0.526 156.h 0.26 0.41 0.38 0.38 0.48 0.38 0.50 0.42 0.44 0.52 0.41 0.53 0.426 850 hPa **RMSE** Table 17 TEMPERATURE Oct Nov Dec 1.2 1.2 1.1 Jul Aug Sep 1.2 1.3 1.2 Jan Feb Mar Apr May Jun Mean 1.18 12.h 1.1 1.0 1.1 1.2 1.2 1.2 2.2 2.1 2.1 2.2 2.5 2.2 2.2 2.0 2.0 2.10 2.7 2.8 2.9 .3.2 3.0 2.5 2.7 2.8 2.6 2.6 60.h 2.4 2.3 84.h 2.8 2.7 3.0 3.2 3.3 3.4 3.3 3.8 3.5 3.3 3.1 3.0 3.19 3.7 108.h 3.2 3.1 3.4 3.5 3.7 3.8 4.13.9 3.4 3.4 3.90 3.9 4.0 4.1 4.5 3.9 132.h 3.5 3.4 3.7 4.1 4.2 3.7 3.6 3.7 4.0 4.1 4.2 4.4 4 4 4.8 4.5 4.2 3.9 3.9 4.16 156.h 3.8 p156.h 4.2 4.6 4.8 4.8 4.9 5.0 5.2 5.4 5.2 5.0 4.8 4.5 4.87 climate 3.4 3.8 4.4 4.7 4.7 4.4 4.6 5.1 4.5 4.2 3.8 3.8 4.30 TEMPERATURE 850 hPa ANOMALY CORRELATION Table 18 Apr May Jun Jul Aug Sep Oct Nov Jan Feb Mar 12.h 0.95 0.96 0.96 0.96 0.97 0.96 0.96 0.96 0.96 0.96 0.95 0.95 0.959 36.h 0.84 0.87 0.88 0.88 0.89 0.87 0.88 0.87 0.88 0.87 0.86 0.86 0.871 0.73 0.79 0.80 0.81 0.82 0.79 0.80 0.78 0.78 0.79 0.77 0.77 0.786 60.h 84.h 0.63 0.71 0.72 0.73 0.74 0.70 0.73 0.70 0.70 0.71 0.68 0.69 0.703 108.h 0.54 0.62 0.64 0.66 0.66 0.62 0.66 0.64 0.63 0.63 0.58 0.61 0.626 0.45 0.55 0.57 0.59 0.61 0.55 0.59 0.57 0.56 0.51 0.54 0.555 156.h 0.35 0.48 0.50 0.55 0.56 0.50 0.53 0.51 0.50 0.51 0.44 0.48 0.495

9. Plans for the future

The next major upgrade of the GME system is planned for the first quarter of the year 2003. The mesh size will be reduced from 60 to 30 km, and the number of layers increased from 31 to 35. For LM, the next major upgrade will be introduced in 2004 with a reduction of mesh size from 7 down to 2.8 km, and an increase of the number of layers from 35 to 45. This high a resolution aims mainly at the explicit prediction of deep convection which is a major forecasting problem in Germany during the warm season. The further development of LM is co-ordinated in the Consortium for Small-Scale Modelling (COSMO). Current members of COSMO are the weather services of Germany, Greece, Italy, Poland and Switzerland

Concerning applications of NWP results it is planned to make a more systematic approach to severe weather forecasting by making use of objective methods based on the EPS provided by the ECMWF. For any kind of postprocessed specialized forecasts of the parameters temperature, wind and significant weather MOS will be used instead of Kalman Filtering.

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